

Square Root Rules

Definitions

1. $b = \sqrt{a}$ if both $b \geq 0$ and $b^2 = a$.

2. $\sqrt{a^2} = |a|$

3. If $a \geq 0$ then;

$$\sqrt{a^2} = a$$

Examples

$$\sqrt{9} = 3 \text{ because } 3^2 = 9.$$

$$\sqrt{(-5)^2} = |-5| = 5$$

$$\sqrt{12^2} = 12$$

Distributing ($a \geq 0$ and $b \geq 0$)

1. $\sqrt{ab} = \sqrt{a}\sqrt{b}$

2. $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$ ($b \neq 0$)

3. $\sqrt{a}\sqrt{a} = a$

Examples

$$\sqrt{18} = \sqrt{9 \cdot 2} = \sqrt{9} \cdot \sqrt{2} = 3\sqrt{2}$$

$$\sqrt{\frac{9}{4}} = \frac{\sqrt{9}}{\sqrt{4}} = \frac{3}{2}$$

$$\sqrt{10}\sqrt{10} = 10$$

Careful!!

1. $\sqrt{a+b} \neq \sqrt{a} + \sqrt{b}$

2. $\sqrt{a-b} \neq \sqrt{a} - \sqrt{b}$

3. $\sqrt{a^2 + b^2} \neq a + b$

Examples

$$\sqrt{6+10} \neq \sqrt{6} + \sqrt{10}$$

$$\sqrt{6-2} \neq \sqrt{6} - \sqrt{2}$$

$$\sqrt{9+4} \neq 3+2$$

Rationalizing the Denominator

$$1. \frac{a}{\sqrt{b}} = \frac{a}{\sqrt{b}} \cdot \frac{\sqrt{b}}{\sqrt{b}} = \frac{a\sqrt{b}}{b}$$

Example

$$\frac{4}{\sqrt{2}} = \frac{4}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{4\sqrt{2}}{2} = 2\sqrt{2}$$

Another Example:

$$\frac{10}{2\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{10\sqrt{5}}{2 \cdot 5} = \frac{10\sqrt{5}}{10} = \sqrt{5}$$